

Artificial Neural Networks for Storm Surge Predictions in NC

DHS Summer Research Team

Outline

- Introduction;
- Feedforward Artificial Neural Network;
- Design questions;
- Implementation;
- Improvements;
- Conclusions;

Brief Introduction

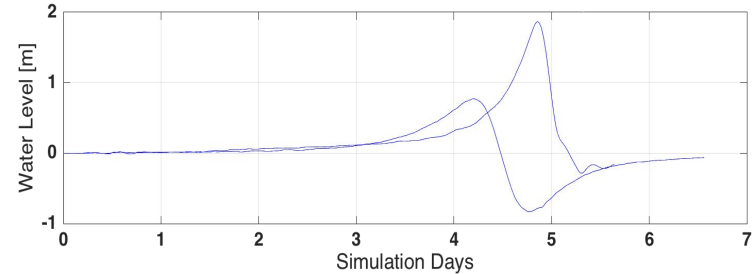
- Anton Bezuglov, Ph.D. in Computer Science and Engineering, University of South Carolina, Columbia, 2006
- Assoc. Professor of Computer Science at Benedict College
- Areas of interests: Machine learning, neural networks, algorithms, etc
- Summer Research Team 2016, sponsored by DHS
- Artificial Neural Networks for Storm Surge Prediction

Brief Introduction, contd.

- Motivation: accurate method for storm surge prediction;
- Parametric vs. Nonparametric approaches (Bishop, 2006)
- Parametric models are computationally expensive;
- Nonparametric models are cheap, but need training;
- Problem: need *large* datasets for training;
- Synthetic hurricanes;

Dataset

- 324 synthetic hurricanes;
- 193 samples per hurricane
- 6 inputs, 10 outputs
- Inputs: hurricane parameters
- Outputs: water levels at 10 locations



```
[bezuglov@ad.renci.org@bb-w540-1 code]$ cat ../data/ann_dataset_10points/track.001.dat
1 -3.000000 -79.0000 28.090 973.4 27.150 1.100 1013.0 0.0054 0.0051 0.0056 0.0059 0.0068 0.0071 0.0114 0.0122 0.0134 0.0167
2 -2.97917 -79.0000 28.130 973.4 27.190 1.100 1013.0 0.0041 0.0048 0.0056 0.0061 0.0058 0.0071 0.0100 0.0108 0.0138 0.0159
3 -2.95833 -79.0000 28.170 973.4 27.230 1.100 1013.0 0.0039 0.0048 0.0055 0.0064 0.0065 0.0073 0.0083 0.0099 0.0133 0.0155
4 -2.93750 -79.005 28.205 973.4 27.260 1.095 1013.0 0.0044 0.0045 0.0056 0.0065 0.0075 0.0066 0.0079 0.0097 0.0128 0.0152
5 -2.91667 -79.010 28.240 973.4 27.290 1.090 1013.0 0.0046 0.0046 0.0058 0.0070 0.0082 0.0059 0.0091 0.0095 0.0116 0.0143
6 -2.89583 -79.010 28.280 973.4 27.330 1.090 1013.0 0.0048 0.0053 0.0062 0.0070 0.0078 0.0071 0.0094 0.0085 0.0097 0.0121
7 -2.87500 -79.010 28.320 973.4 27.370 1.090 1013.0 0.0056 0.0061 0.0066 0.0063 0.0071 0.0084 0.0087 0.0087 0.0085 0.0112
8 -2.85417 -79.015 28.355 973.4 27.405 1.090 1013.0 0.0062 0.0064 0.0066 0.0063 0.0069 0.0085 0.0093 0.0097 0.0089 0.0105
9 -2.83333 -79.020 28.390 973.4 27.440 1.090 1013.0 0.0062 0.0062 0.0063 0.0069 0.0074 0.0081 0.0112 0.0101 0.0104 0.0104
10 -2.81250 -79.020 28.430 973.4 27.475 1.090 1013.0 0.0057 0.0056 0.0064 0.0069 0.0083 0.0079 0.0119 0.0120 0.0107 0.0123
11 -2.79167 -79.020 28.470 973.4 27.510 1.090 1013.0 0.0047 0.0053 0.0067 0.0068 0.0082 0.0082 0.0118 0.0140 0.0116 0.0150
12 -2.77083 -79.025 28.505 973.4 27.545 1.090 1013.0 0.0043 0.0052 0.0063 0.0065 0.0074 0.0089 0.0119 0.0138 0.0137 0.0170
13 -2.75000 -79.030 28.540 973.4 27.580 1.090 1013.0 0.0046 0.0052 0.0061 0.0064 0.0072 0.0094 0.0123 0.0124 0.0163 0.0180
14 -2.72917 -79.030 28.580 973.4 27.620 1.090 1013.0 0.0050 0.0054 0.0061 0.0065 0.0077 0.0091 0.0118 0.0126 0.0171 0.0191
15 -2.70833 -79.030 28.620 973.4 27.660 1.090 1013.0 0.0053 0.0057 0.0062 0.0067 0.0081 0.0085 0.0116 0.0129 0.0156 0.0208
16 -2.68750 -79.035 28.655 973.4 27.695 1.090 1013.0 0.0054 0.0061 0.0062 0.0065 0.0080 0.0080 0.0123 0.0128 0.0150 0.0205
17 -2.66667 -79.040 28.690 973.4 27.730 1.090 1013.0 0.0060 0.0064 0.0061 0.0061 0.0076 0.0075 0.0114 0.0131 0.0157 0.0189
18 -2.64583 -79.040 28.730 973.4 27.770 1.090 1013.0 0.0060 0.0064 0.0057 0.0060 0.0073 0.0082 0.0105 0.0119 0.0154 0.0177
19 -2.62500 -79.040 28.770 973.4 27.810 1.090 1013.0 0.0058 0.0061 0.0058 0.0065 0.0073 0.0085 0.0102 0.0104 0.0136 0.0165
```

inputs

outputs

Assumption

- Based on previous studies;
- Suppose input -- $\mathbf{x}(t)$, output -- $\mathbf{y}(t)$, t - time;
- $\mathbf{x}(t)$ contains all information to make predictions
- $\mathbf{y}(t)$ depends on $\mathbf{x}(t)$ *only*
- $\mathbf{y}(t)$ does *not* depend on $\mathbf{x}(t-1)$, $\mathbf{y}(t-1)$, etc.

```
[bezuglov@ad.renci.org@bb-w540-1 code]$ cat ../data/ann_dataset_10points/track.001.dat
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3 -2.95833 -79.000 28.170 973.4 27.230 1.100 1013.0 0.0039 0.0048 0.0055 0.0064 0.0065 0.0073 0.0083 0.0099 0.0133 0.0155
4 2.02750 -79.005 28.205 973.4 27.260 1.095 1013.0 0.0044 0.0045 0.0056 0.0065 0.0075 0.0066 0.0070 0.0097 0.0120 0.0150
5 -2.91667 -79.010 28.240 973.4 27.290 1.090 1013.0 0.0046 0.0046 0.0058 0.0070 0.0082 0.0059 0.0091 0.0095 0.0116 0.0143
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8 -2.85417 -79.015 28.355 973.4 27.405 1.090 1013.0 0.0062 0.0064 0.0066 0.0063 0.0069 0.0085 0.0093 0.0097 0.0089 0.0105
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17 -2.66667 -79.040 28.690 973.4 27.730 1.090 1013.0 0.0060 0.0064 0.0061 0.0061 0.0076 0.0075 0.0114 0.0131 0.0157 0.0189
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19 -2.62500 -79.040 28.770 973.4 27.810 1.090 1013.0 0.0058 0.0061 0.0058 0.0065 0.0073 0.0085 0.0102 0.0104 0.0136 0.0165
```

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Regression with a FF ANN

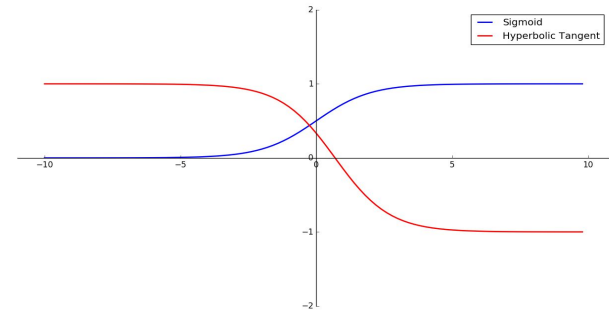
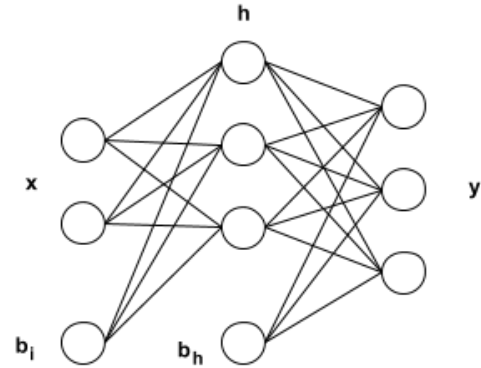
- Problem: find a function $f(\cdot)$, so that:
- $\mathbf{y}_p = f(\mathbf{x})$, \mathbf{y}_p -- storm surge predictions
- $f(\cdot)$ -- can be a Feed Forward Artificial Neural Network (FF ANN);
- Train FF ANN to minimize the error between \mathbf{y} and \mathbf{y}_p
- Use synthetic storms to train;

FF ANN's

- One hidden layer ANN, two layer model;
- Information travels from left to right;
- Nodes are variables (inputs, outputs, and hidden);
- Edges -- independent parameters;
- Nonlinear function;
- Complexity determined by # of multiplications
- Approx. $O(N^2)$, N - # of hidden nodes
- Backpropagation algorithm

$$f(\mathbf{x}) = W_h * \mathbf{h} + \mathbf{b}_h$$

$$\mathbf{h} = \sigma(W_i * \mathbf{x} + \mathbf{b}_i)$$



Design Questions

- Architecture?
- Number of hidden layers?
- Size of each layer?
- Choice of nonlinear function?
- Initial weights/biases?
- Learning rate?
- Learning rate decay?
- Algorithm for training?
- Clipping gradients?
- Dealing with overfitting?
- Loss function?

Design Questions, contd.

- Architecture? -- *Two hidden layer multiple outputs*
- Number of hidden layers? -- *two hidden layers*
- Size of each layer? -- *16-64 neurons, second layer larger*
- Choice of nonlinear function? -- *TanH*
- Initial weights/biases? -- *$N(0, 0.01)$*
- Learning rate? -- *0.001 -- 0.01*
- Learning rate decay? -- *0.5*
- Algorithm for training? -- *ADAM optimization algorithm*
- Clipping gradients? -- *yes, 1.25-1.5 norm*
- Dealing with overfitting? -- *validation set, 15%*
- Loss function-- *Mean Squared Error (MSE)*

Design Questions, contd.

- Stochastic optimization
 - Use portions of the training dataset: batches
 - Training dataset: 228 storms, batches: 19, 57, 114
 - Or Training dataset: 225 storms, batches: 3, 5, 9, 15, 45, 225
- Inputs normalization
 - Inputs vary by 2-3 orders of magnitude
 - Too long to converge
 - Calculate moments for each input param in the training dataset
 - Normalize inputs
 - Store the moments along with the model

Design Summary

- Split dataset into training (70%), validation (15%), and testing (15%);
- Two hidden layer FF ANN ($N_1 < N_2$, less inputs than outputs);
- Train to minimize MSE;
- Check for overfitting on the validation dataset;
- Evaluate performance on the testing dataset;

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Implementation: TensorFlow

- TensorFlow -- Open Source Library for Machine Intelligence;
- Algorithms are graphs, nodes -- operations, edges -- tensors

```
tf_train_dataset = tf.placeholder(tf.float32, shape=(batch_size, 6)) #train_dataset2.shape(2)
tf_train_labels = tf.placeholder(tf.float32, shape=(batch_size, 2))
tf_valid_dataset = tf.constant(valid_dataset2)
tf_test_dataset = tf.constant(test_dataset2)

weights_0 = tf.Variable(tf.truncated_normal([6,hidden_nodes_1], dtype = tf.float32))
biases_0 = tf.Variable(tf.zeros([hidden_nodes_1], dtype = tf.float32))

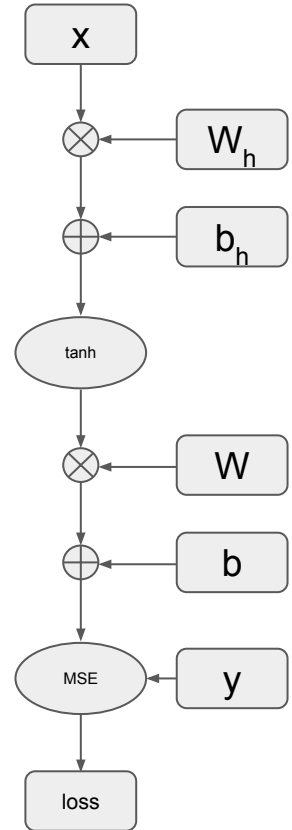
weights_1 = tf.Variable(tf.truncated_normal([hidden_nodes_1,hidden_nodes_2], dtype = tf.float32))
biases_1 = tf.Variable(tf.zeros([hidden_nodes_2], dtype = tf.float32))

weights_2 = tf.Variable(tf.truncated_normal([hidden_nodes_2,2], dtype = tf.float32))
biases_2 = tf.Variable(tf.zeros([2], dtype = tf.float32))

input_layer_output = tf.sigmoid(tf.matmul(tf_train_dataset, weights_0) + biases_0)
hidden_layer_output = tf.sigmoid(tf.matmul(input_layer_output, weights_1) + biases_1)
#hidden_layer_output = tf.nn.dropout(hidden_layer_output, 0.5)
hidden_layer_output = tf.matmul(hidden_layer_output, weights_2) + biases_2

loss = tf.cast(tf.reduce_mean(tf.reduce_mean(tf.square(hidden_layer_output-tf_train_labels))),tf.float32)
#loss = tf.cast(tf.reduce_mean(tf.reduce_mean(tf.square(tf.square(hidden_layer_output-tf_train_labels)))),tf.float32)

global_step = tf.Variable(0.00, trainable=False)
learning_rate = tf.train.exponential_decay(starter_learning_rate, global_step, num_steps, 0.96, staircase=False)
optimizer = tf.train.GradientDescentOptimizer(learning_rate).minimize(loss, global_step=global_step)
```



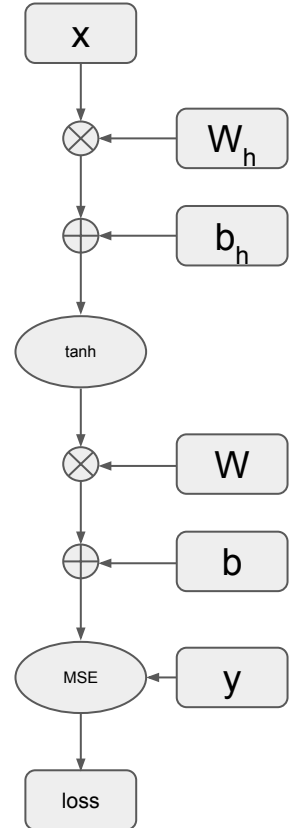
Implementation: Training and Evaluation

- Graph variables can be evaluated/called
- To train -- call optimizer variable
- To evaluate -- call loss variable
- etc.

```
batch_data = train_dataset2[offset:(offset + batch_size), :]  
batch_output = train_output[offset:(offset + batch_size), :]  
feed_dict = {tf_train_dataset : batch_data, tf_train_labels : batch_output}  
_, l, predictions = session.run([optimizer, loss, train_prediction], feed_dict=feed_dict)
```

List of graph variables to evaluate

Inputs for placeholders



Implementation: Dealing with Gradients

Calculate
gradients

Clip

Apply gradients

Evaluate
train_op to
perform a single
train iteration

```
# Training portion of the graph
# Eval train_op to perform one step training to minimize loss
#=====
# Prepare global step and learning rate for optimization
global_step = tf.get_variable(
    'global_step', [],
    initializer=tf.constant_initializer(0), trainable=False)
learning_rate = tf.train.exponential_decay(
    FLAGS.learning_rate, global_step, FLAGS.max_steps,
    FLAGS.learning_rate_decay, staircase=False)

# Create ADAM optimizer
optimizer = tf.train.AdamOptimizer(learning_rate)

# Calculate gradients and apply them
grads, v = zip(*optimizer.compute_gradients(loss))
grads, _ = tf.clip_by_global_norm(grads, 1.25)
apply_gradient_op = optimizer.apply_gradients(zip(grads,v), global_step = global_step)

# Smoothen variables after gradient applications
variable_averages = tf.train.ExponentialMovingAverage(
    FLAGS.moving_avg_decay, global_step)
variables_averages_op = variable_averages.apply(tf.trainable_variables())
train_op = tf.group(apply_gradient_op, variables_averages_op)]

init = tf.initialize_all_variables()
sess = tf.Session(config = tf.ConfigProto(
    allow_soft_placement = False, # allows to utilize GPU's & CPU's
    log_device_placement = False)) # shows GPU/CPU allocation
```

Implementation: Multiple GPU's

- Each GPU has same graph but individual inputs/outputs;
- Calculate gradients on each GPU;
- Average gradient;
- Apply gradients;
- Update graphs;

Algorithm 1 Training algorithm for a multiple output ANN on parallel GPU's using TensorFlow

```
1: procedure TRAIN( $\mathbf{x}, \hat{\mathbf{y}}$ ) ▷  $\mathbf{x}$  – inputs,  $\hat{\mathbf{y}}$  – observations
2:    $\mathbf{x}_n = \text{Normalize}(\mathbf{x})$  ▷ subtract means and divide by std component-wise
3:   for  $g$  in GPUs do
4:      $g \leftarrow \text{InitializeNetwork}()$  ▷ Assign a copy of the network on each GPU
5:   end for
6:   for  $e$  in Epochs do
7:      $b_{1..GPU_s} \leftarrow \text{GetDataBatch}(\mathbf{x}_n, \hat{\mathbf{y}}, size)$  ▷ Fetch batches of training data for each GPU
8:      $g_{1..GPU_s} \leftarrow \text{CalculateGradients}(b_{1..GPU_s})$  ▷ Calculate gradients on each GPU
9:      $g \leftarrow \text{Mean}(g_{1..GPU_s})$  ▷ Find average gradient
10:     $\mathbf{v} \leftarrow \text{AdamOptimizer}(g, rate)$  ▷ Obtain the new values of network parameters
11:    UpdateNetworks( $\mathbf{v}$ ) ▷ Propagate changes to all networks
12:  end for
13: end procedure
```

Implementation: Restore ANN

- Save model: *weights, biases, and input moments*;
- Train/Run modes;
- Train -- open file, train ANN, save ANN;
- Run -- open file, open model, run, save outputs;
- Train, approx. 1-20 minutes;
- Run, 0.11 sec (324x193 samples);

```
[bezuglov@ad.renci.org@bb-w540-1 code]$ python ./ilt_default_feed.py
Processed 0/324

Processed 100/324

Processed 200/324

Processed 300/324

inputs: calculate new means, stds for dataset with 44004 samples
outputs: calculate new means, stds for dataset with 44004 samples
normalizing inputs and outputs
inputs: using provided means, stds for dataset with 9264 samples
outputs: using provided means, stds for dataset with 9264 samples
normalizing inputs and outputs
inputs: using provided means, stds for dataset with 9264 samples
outputs: using provided means, stds for dataset with 9264 samples
normalizing inputs and outputs
Num hurricanes in train 228, validation 48, test 48
Step 0 (83.63 op/sec): Training MSE: 0.22264, Validation CC: 0.0051, MSE: 0.12320
Step 2500 (229.94 op/sec): Training MSE: 0.02879, Validation CC: 0.0781, MSE: 0.02115
Step 5000 (236.97 op/sec): Training MSE: 0.01371, Validation CC: 0.9163, MSE: 0.01313
Step 7500 (220.66 op/sec): Training MSE: 0.01001, Validation CC: 0.9320, MSE: 0.01122
Step 10000 (201.46 op/sec): Training MSE: 0.00859, Validation CC: 0.9402, MSE: 0.01026
Step 12500 (213.17 op/sec): Training MSE: 0.00767, Validation CC: 0.9437, MSE: 0.00956
Step 15000 (215.19 op/sec): Training MSE: 0.00697, Validation CC: 0.9496, MSE: 0.00867
Step 17500 (221.53 op/sec): Training MSE: 0.00651, Validation CC: 0.9487, MSE: 0.00874
Step 20000 (221.29 op/sec): Training MSE: 0.00623, Validation CC: 0.9505, MSE: 0.00838
Step 22500 (214.64 op/sec): Training MSE: 0.00595, Validation CC: 0.9509, MSE: 0.00822
Step 25000 (215.57 op/sec): Training MSE: 0.00571, Validation CC: 0.9526, MSE: 0.00804
Step 27500 (211.51 op/sec): Training MSE: 0.00562, Validation CC: 0.9527, MSE: 0.00799
Step 30000 (205.55 op/sec): Training MSE: 0.00543, Validation CC: 0.9538, MSE: 0.00795
Step 32500 (210.79 op/sec): Training MSE: 0.00541, Validation CC: 0.9540, MSE: 0.00782
Step 35000 (210.35 op/sec): Training MSE: 0.00526, Validation CC: 0.9552, MSE: 0.00782
Step 37500 (222.17 op/sec): Training MSE: 0.00515, Validation CC: 0.9555, MSE: 0.00780
Step 40000 (214.22 op/sec): Training MSE: 0.00503, Validation CC: 0.9555, MSE: 0.00761
Step 42500 (212.13 op/sec): Training MSE: 0.00494, Validation CC: 0.9548, MSE: 0.00764
Step 45000 (212.13 op/sec): Training MSE: 0.00486, Validation CC: 0.9563, MSE: 0.00766
Step 47500 (211.01 op/sec): Training MSE: 0.00475, Validation CC: 0.9565, MSE: 0.00750
Step 50000 (214.69 op/sec): Training MSE: 0.00469, Validation CC: 0.9564, MSE: 0.00759
Training summary:
Test MSE: 0.00769
Location 0: CC: 0.9511, MSE: 0.002691
Location 1: CC: 0.9616, MSE: 0.002060
Location 2: CC: 0.9713, MSE: 0.001207
Location 3: CC: 0.9751, MSE: 0.000948
Location 4: CC: 0.9670, MSE: 0.003165
Location 5: CC: 0.9334, MSE: 0.005563
Location 6: CC: 0.9678, MSE: 0.009057
Location 7: CC: 0.9377, MSE: 0.025910
Location 8: CC: 0.9204, MSE: 0.010701
Location 9: CC: 0.9369, MSE: 0.015614
```

```
[bezuglov@ad.renci.org@bb-w540-1 code]$ python ./ilt_default_feed.py
Model ./models/save_two_layers_32_64_15000_AB/model.ckpt-50000 restored
Elapsed time: 0.11 sec.
Outputs saved as ./test_track_out2.dat
[bezuglov@ad.renci.org@bb-w540-1 code]$
```

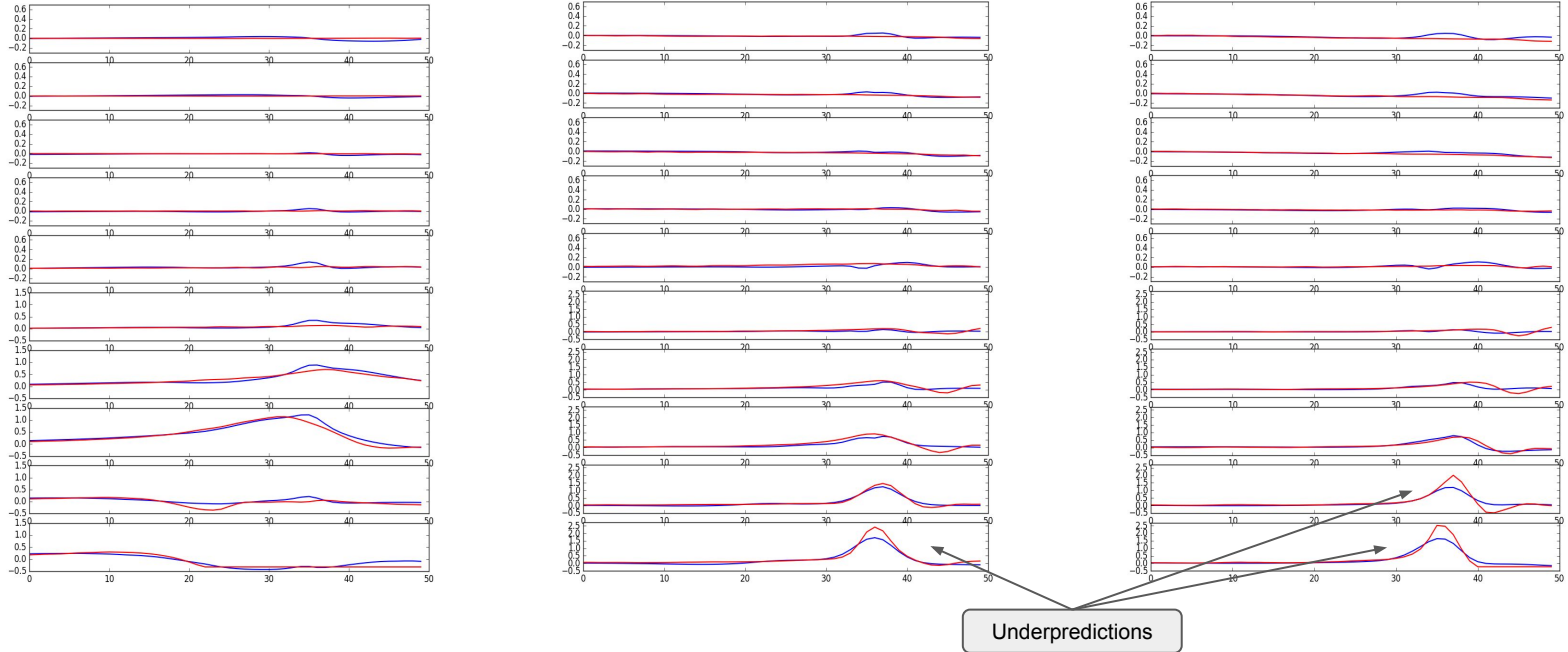
FF ANN: Performance

- Two hidden layer FF ANN (32,64)

Location	MSE	R	$P(e \leq 0.1m)$	$e^*, P(e \leq e^*) = 0.95$	$P(e \leq 0.1m)$	$P(e \leq 0.5m)$
1	0.0017	0.963	0.966	0.15	0.864	0.998
2	0.0012	0.975	0.976	0.13	0.909	0.998
3	0.0008	0.988	0.992	0.10	0.950	0.999
4	0.0004	0.992	0.993	0.10	0.953	0.999
5	0.0014	0.976	0.978	0.17	0.861	0.994
6	0.0038	0.932	0.935	0.32	0.692	0.985
7	0.0079	0.892	0.900	0.46	0.531	0.960
8	0.0112	0.853	0.864	0.51	0.477	0.949
9	0.0095	0.901	0.910	0.44	0.566	0.960
10	0.0175	0.833	0.850	0.49	0.475	0.953

FF ANN: Performance

ADCIRC
FF ANN



FF ANN: Summary

- Multi-output ANN: one model for several locations
- MSE's are approx. 0.006 m²
- CC's are 0.95
- ANN has no error *before* and *after* the storm surge;
- Larger errors at storm surge;
- Low MSE's b/c of zeros;

Does $y(t)$ depend on $x(t)$ *and* something else?

Does $x(t)$ miss information?

Assumption

- Based on previous studies;
- Suppose input $x(t)$, output $y(t)$, t -time;
- $x(t)$ contains all information to make predictions
- $y(t)$ depends on $x(t)$ only
- $y(t)$ does not depend on $x(t-1)$, $x(t-2)$, etc.



Time	Input	Output
1	0.0	0.0
2	0.0	0.0
3	0.0	0.0
4	0.0	0.0
5	0.0	0.0
6	0.0	0.0
7	0.0	0.0
8	0.0	0.0
9	0.0	0.0
10	0.0	0.0
11	0.0	0.0
12	0.0	0.0
13	0.0	0.0
14	0.0	0.0
15	0.0	0.0
16	0.0	0.0
17	0.0	0.0
18	0.0	0.0
19	0.0	0.0
20	0.0	0.0
21	0.0	0.0
22	0.0	0.0
23	0.0	0.0
24	0.0	0.0
25	0.0	0.0
26	0.0	0.0
27	0.0	0.0
28	0.0	0.0
29	0.0	0.0
30	0.0	0.0
31	0.0	0.0
32	0.0	0.0
33	0.0	0.0
34	0.0	0.0
35	0.0	0.0
36	0.0	0.0
37	0.0	0.0
38	0.0	0.0
39	0.0	0.0
40	0.0	0.0
41	0.0	0.0
42	0.0	0.0
43	0.0	0.0
44	0.0	0.0
45	0.0	0.0
46	0.0	0.0
47	0.0	0.0
48	0.0	0.0
49	0.0	0.0
50	0.0	0.0
51	0.0	0.0
52	0.0	0.0
53	0.0	0.0
54	0.0	0.0
55	0.0	0.0
56	0.0	0.0
57	0.0	0.0
58	0.0	0.0
59	0.0	0.0
60	0.0	0.0
61	0.0	0.0
62	0.0	0.0
63	0.0	0.0
64	0.0	0.0
65	0.0	0.0
66	0.0	0.0
67	0.0	0.0
68	0.0	0.0
69	0.0	0.0
70	0.0	0.0
71	0.0	0.0
72	0.0	0.0
73	0.0	0.0
74	0.0	0.0
75	0.0	0.0
76	0.0	0.0
77	0.0	0.0
78	0.0	0.0
79	0.0	0.0
80	0.0	0.0
81	0.0	0.0
82	0.0	0.0
83	0.0	0.0
84	0.0	0.0
85	0.0	0.0
86	0.0	0.0
87	0.0	0.0
88	0.0	0.0
89	0.0	0.0
90	0.0	0.0
91	0.0	0.0
92	0.0	0.0
93	0.0	0.0
94	0.0	0.0
95	0.0	0.0
96	0.0	0.0
97	0.0	0.0
98	0.0	0.0
99	0.0	0.0
100	0.0	0.0

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